Part IV

Iconic and pixel based displays

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Outline

Introduction

Iconic displays

- Chernoff's faces
- Star glyph
- Glyph Positioning
- Pixel based displays
 Dense pixel displays
 Dissimilarity matrix

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Two opposite ways of addressing scalability issues:

- Glyph/Iconic displays:
 - Scatter plot "dots" are replaced by rich icon or glyphs
 - Locality is enforced: all characteristics of an object are mapped in a small area of the display
- Pixel based displays:
 - A numerical value is mapped to a single pixel
 - Displays are dense: nothing is "vasted"

10 Introduction

Iconic displays

- Chernoff's faces
- Star glyph
- Glyph Positioning

Pixel based displays Dense pixel display

Dissimilarity matrix

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Replacing dots by icons or glyphs:

- Each object is represented by an icon
- Variations in shape/color/etc. of the icon encode variables
- Icon position:
 - Structure driven
 - Data driven
- Examples:
 - Chernoff's faces
 - Star glyph
 - Stick-figure icon
 - etc.

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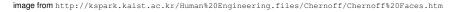
Pros:

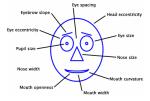
- complete independent display of each object
- pre-attentive processing
- can be very intuitive (good learning curve)
- Cons:
 - glyph design
 - variable mapping: important variation in feature expressive power
 - glyph positioning
 - glyph overlapping

Chernoff's faces

Proposed by Chernoff in 1973:

- Values mapped to characteristics of faces:
 - eyes, nose, mouth, ears, head, hair, eyebrows, etc.
 - position, size, curvature, etc.
 - combined with color
- Pros:
 - Easy to understand
 - Can convey strong messages
- Cons:
 - Numerous variants
 - Strongly depends on the chosen characteristics
 - Uses a lot of screen surface

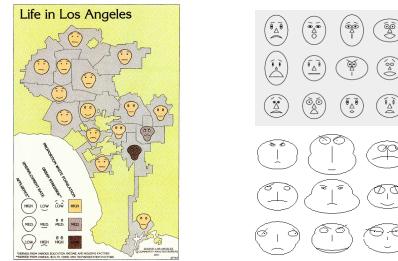




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Examples



http://kspark.kaist.ac.kr/Human%20Engineering.files/Chernoff/Chernoff%20Faces.htm http://mathworld.wolfram.com/ChernoffFace.html http://aoki2.si.gunma-u.ac.jp/R/face.html

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Anderson's/Fisher's Iris

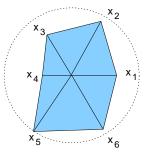
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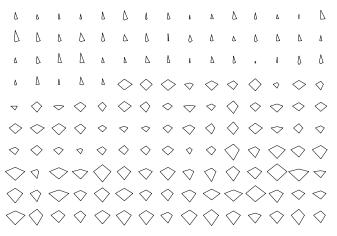
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Proposed by Siegel, Farrell, Goldwyn & Friedman in 1972:

- *p* variables are mapped to a polygon with *p* - 1 edges (*p* vertices)
- the distance between the center and vertex *i* is proportional to *x_i*
- radii are optional
- corresponds to individual polar parallel coordinates





Anderson's/Fisher's Iris

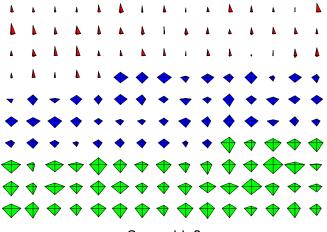
Obviously two classes

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Iris

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Obviously two classes														

Anderson's/Fisher's Iris



Anderson's/Fisher's Iris

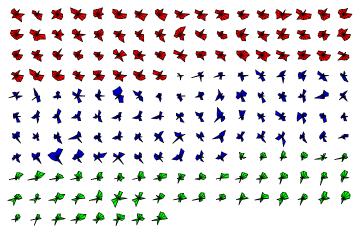
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Glyph Positioning

Anderson's/Fisher's Iris

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Class based order: two classes

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Glyph Positioning

Anderson's/Fisher's Iris

Random order: no structure

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- Strong impact on perception
- Two classes of algorithms:
 - Structure driven:
 - Prior choice of a structure (e.g., a grid)
 - Layout in the structure can be data driven (ordering)
 - Data driven:
 - Positions of the glyphs is extracted from the data
 - User guided (scatter plot like)
 - Automated (e.g., via a projection)
- Overlapping is a major problem:
 - Additional constraints for data driven solution
 - Rendering solutions (transparency, auto-size, post processing)

Based on a prior structure

- No overlapping
- "Reading order"
- Glyph ordering:
 - A seriation problem (like variable ordering)
 - User guided (target variable, chosen input variable, etc.): also called query based order
 - Automated:
 - Minimize a dissimilarity between close glyphs
 - NP complete
 - Heuristics

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Structure driven with user ordering

Boston Housing (UCI)

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Structure driven with user ordering

Boston Housing (UCI), Target ordered

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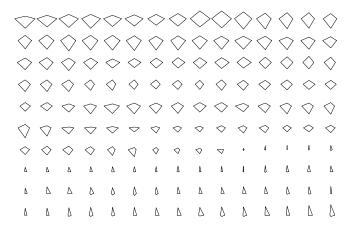
Structure driven with automated ordering

Anderson's/Fisher's Iris

Random order: no structure

Structure driven with automated ordering

Anderson's/Fisher's Iris



Hierarchical clustering based order: two classes

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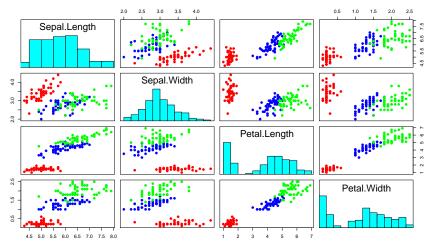
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Based on the data

- Coordinates of glyphs are computed from the data
- User guided:
 - Choose two variables among p
 - Scatter plot of the glyphs
- Automated: projection based approaches
- Overlapping:
 - Rendering (as for scatter plots)
 - Built in prevention (e.g., SOM, Relational Perspective Map)
 - Post processing:
 - Jitter, GridFit, Force directed placement, etc.
 - Adapted size: small glyphs in dense area, larger ones in empty places
 - Zooming interface and clustering

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Data driven under user control

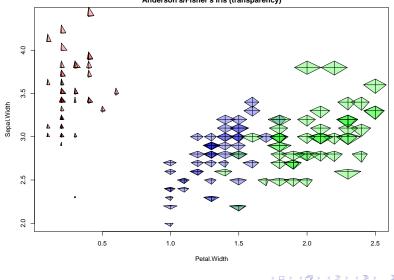


Anderson's/Fisher's Iris

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Data driven under user control

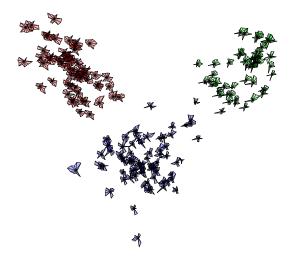


Anderson's/Fisher's Iris (transparency)

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Automated data driven

Italian Wines (LDA + transparency)

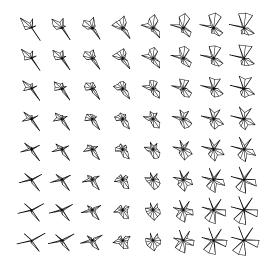


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Automated data driven

Self Organizing Map (Boston Housing)



Post-processing

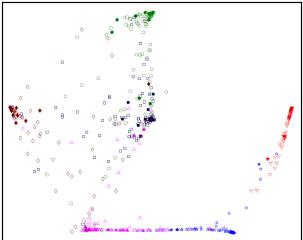
Reducing overlapping after positioning

- Optimization problem:
 - original glyph positions: x_i
 - new positions: y_i
 - movement minimization: $y_i \simeq x_i$
 - overlapping minimization: $y_i \neq y_j$ when $i \neq j$
- Objective function

$$E(\mathbf{y}) = \sum_{i=1}^{n} \|y_i - x_i\|^2 + \eta \sum_{i \neq j} \exp\left(-\frac{\|y_i - y_j\|^2}{2\sigma^2}\right)$$

- η: trade off between faithfulness and overlapping (σ: overlapping radius)
- N-body like problem (frequent also in projection)

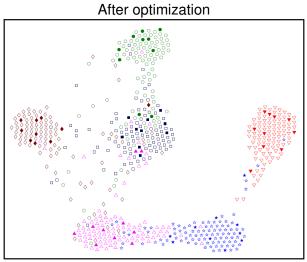
Original layout



from "Visual nonlinear discriminant analysis for classifier design" by Iwata et al., ESANN 2006

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from "Visual nonlinear discriminant analysis for classifier design" by Iwata et al., ESANN 2006

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10 Introduction

Iconic displays

- Chernoff's faces
- Star glyph
- Glyph Positioning

Pixel based displaysDense pixel displays

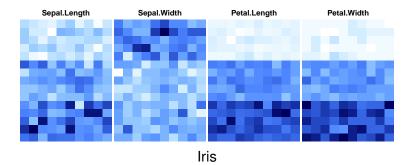
Dissimilarity matrix

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Dense pixel displays

- One pixel per value
- *n* objects with *p* variables \Rightarrow *n* × *p* pixels
- Values are color coded
- One block of pixels per variable

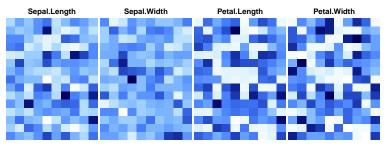


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Dense pixel displays

Pros:

- Very good scalability
- No overlapping
- Pre-attentive processing
- Cons:
 - Extremely order dependent



Iris (random order)

F. Rossi (INRIA)
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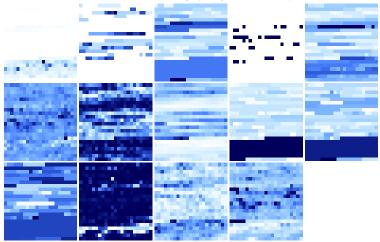
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Two distinct problems

- Pixel layout for one variable:
 - Object order (user chosen or based on seriation)
 - Order mapping: grid "reading order" (same problem for glyphs)
- Variable layout:
 - "Related" variables should be close
 - Problem already encountered for parallel coordinates
 - NP complete

User directed pixel ordering

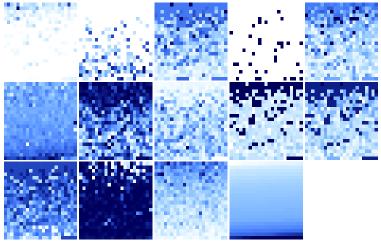
Boston Housing (no pixel order)



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User directed pixel ordering

Boston Housing (target pixel order)



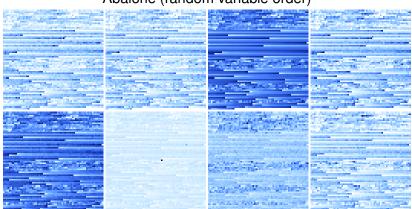
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Automatic ordering

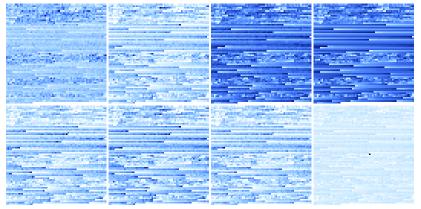


Abalone (random variable order)

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Automatic ordering

Abalone (ordered variables)



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Automatic ordering

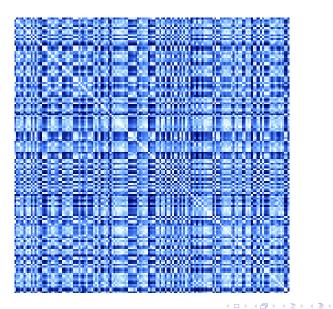
Abalone (ordered on variables and pixels)

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- Pairwise (dis)similarities between objects
- One pixel per dissimilarity: n^2 pixels $(\frac{n(n-1)}{2})$
- Square matrix display
- Values are color coded
- Ordering is mandatory:
 - random order gives random results
 - many different objective functions:
 - correlation between matrix rows
 - "small" diagonal
 - etc.
 - YAFSP (Yet Another Family of Seriation Problems)
 - YAFNPCP (Yet Another Family NP Complete Problems)

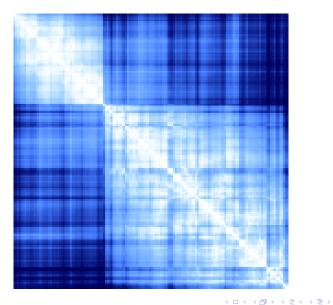


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Iris dataset

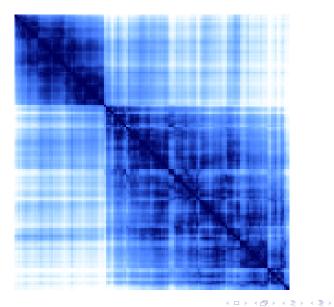


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Iris dataset



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Infovis & ML

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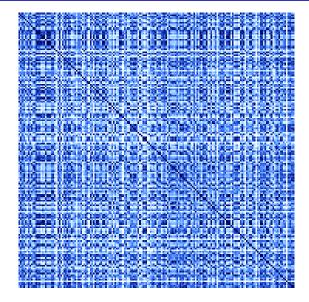
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• Pros:

- Dimension Independent (but beware of distances problems in high dimension)
- Applies to non vector data
- Clustering analysis
- Outlier detection
- Cons:
 - Ordering algorithm are costly (NP complete!)
 - Scalability impaired by ordering costs and by screen occupation
 - Results depends on many parameters:
 - Dissimilarity
 - Ordering criterion
 - Ordering method
 - Color map
 - Usability has not been studied

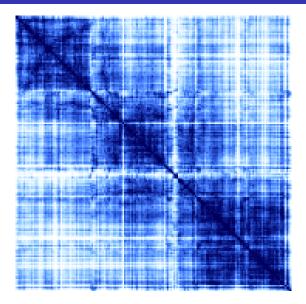
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Random order

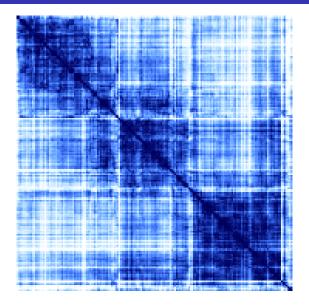


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Correlation similarity, complete linkage, optimal leaf order

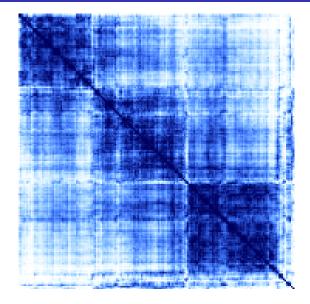


Correlation similarity, average linkage, optimal leaf order



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Euclidean dissimilarity, average linkage, optimal leaf order



Euclidean dissimilarity, average linkage, optimal leaf order, linear color map

